

Multiple choice Circle only one letter for the correct answer!

Question: What is the mean (approximately), the median, and the mode of the following sequence, respectively?

[9, 4, 5, 10, 4, 2, 9, 11, 9, 5, 7, 3, 4, 6, 5, 6, 9]

- a. 5.95, 6, 9 b. 6.35, 6, 9 c. 5.95, 9, 6 d. 6.35, 6, 9 e. 6.05, 9, 6

Question: In a Computer Science Department, three awards (research, teaching, and service) will be given to a class of 75 graduate students. If each student can receive at most one award, how many possible selections are there?

- a. $75!/3!$ b. $75!/(75-3)!$ c. 3^{75} d. $75!/(3!*72!)$ e. 3×75

Question: Suppose that there are 450 people in a village, 250 of which are Female and 200 of which are male. 20 males and 130 females are unemployed. One of these individuals is to be selected at random. We define the following events:

M : a man is chosen,

E : the one chosen is employed.

One person is randomly selected and given that the chosen person is employed, what is the probability that the chosen person is male, i.e. $P(M | E)$?

- a. $5/9$ b. $2/15$ c. $13/15$ d. $7/30$ e. $23/30$

Question: The ABC-XYZ Department puts projects out on bid and generally estimates what a reasonable bid should be. Call the estimate a . The Department has determined that the density function of the winning (i.e. low) bid is

$$f(x) = \begin{cases} \frac{5}{8}a, & \frac{2}{5}a \leq x \leq 2a, \\ 0, & \text{elsewhere.} \end{cases}$$

What is the probability that the winning bid is less than the Department's preliminary estimate a ?

- a. $1/8$ b. $1/4$ c. $3/8$ d. $1/2$ e. $5/8$

Question: If X and Y are random variables with variances $\text{var}(X)=2$ and $\text{var}(Y)=3$ and covariance $\text{cov}(X,Y) = -2$, find the variance of the random variable $Z = 3X - 2Y + 5$.

- a. 6 b. 18 c. 24 d. 30 e. 54

Question: Suppose that we are measuring the glucose intake in 114 regions of the brain using a PET image before and after taking a tests drug *testodamine*. We would like to measure whether there is significant *increase* in the glucose intake overall in these brain regions. What kind of a statistical significance test, among the following, makes sense?

- a. two-sided, unpaired t-test
b. one-sided, unpaired t-test
c. two-sided, paired t-test
d. one-sided, paired t-test
e. it does not make a difference, all would yield the same result

Other Questions. Show your steps. Write legibly.

Question: Let X be a random variable with expected value $E(X) = \mu$.

Prove that, its variance, σ^2 , is equal to $E(X^2) - \mu^2$.

Question: In the NBA (National Basketball Association), in Texas the Mavs-Spurs rivalry is well-known. Based on the history of records of the two teams against each other, the probability of Spurs winning was 62% before the 2013-2014 play-off series. (In basketball, there are two outcomes of a game, either win or lose, there is no tie). When the two teams face each other in a playoff series, the first team to have 4 wins over the other one would win the series.

- What is the minimum and maximum number of games that these two teams can play in the series?
- Given the Spurs' probability of winning vs Mavs above, what is the probability that the Spurs will win the series in 4 games?
- Given the Spurs' probability of winning vs Mavs above, what is the probability that the Spurs will win the series in 5 games?
- Given the Spurs' probability of winning vs Mavs above, what is the probability that the Spurs will win the series in 6 games?
- Given the Spurs' probability of winning vs Mavs above, what is the probability that the Spurs will win the series in 7 games?

Question: A company which manufactures light bulbs which have a lifetime (before a burnout) that is normally distributed with mean equal to 800 hours and a standard deviation of 40 hours. Using the attached "Area Under Normal Curve" table provided in the last page, calculate:

- Find the probability that a bulb manufactured by this company burns more than 868 hours.
- Find the probability that a bulb manufactured by this company burns less than 732 hours.

